



Business Statistics: A Decision-Making Approach

6th Edition

Chapter 13

Introduction to Linear Regression and Correlation Analysis



Chapter Goals

After completing this chapter, you should be able to:

- Calculate and interpret the simple correlation between two variables
- Determine whether the correlation is significant
- Calculate and interpret the simple linear regression equation for a set of data
- Understand the assumptions behind regression analysis
- Determine whether a regression model is significant



Chapter Goals

(continued)

After completing this chapter, you should be able to:

- Calculate and interpret confidence intervals for the regression coefficients
- Recognize regression analysis applications for purposes of prediction and description
- Recognize some potential problems if regression analysis is used incorrectly
- Recognize nonlinear relationships between two variables



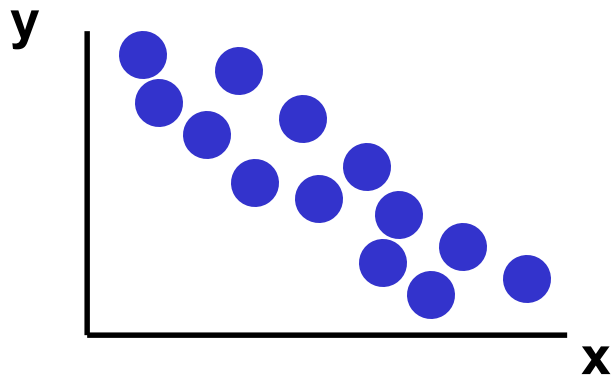
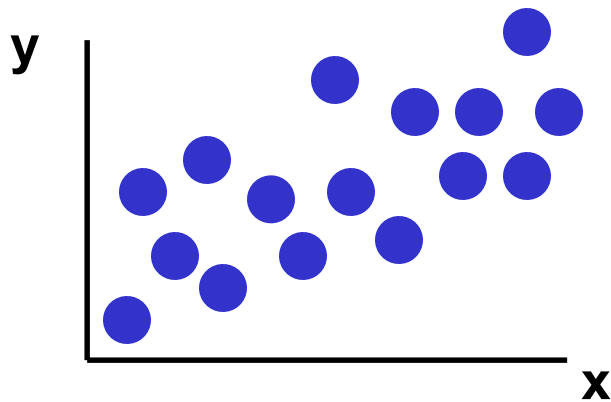
Scatter Plots and Correlation

- A **scatter plot** (or scatter diagram) is used to show the relationship between two variables
- **Correlation** analysis is used to measure strength of the association (linear relationship) between two variables
 - Only concerned with strength of the relationship
 - No causal effect is implied

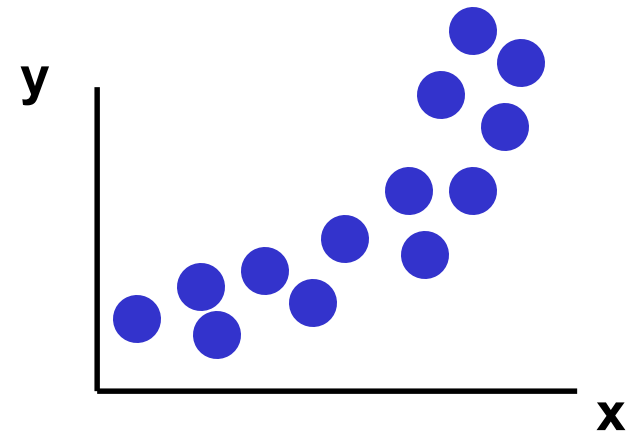
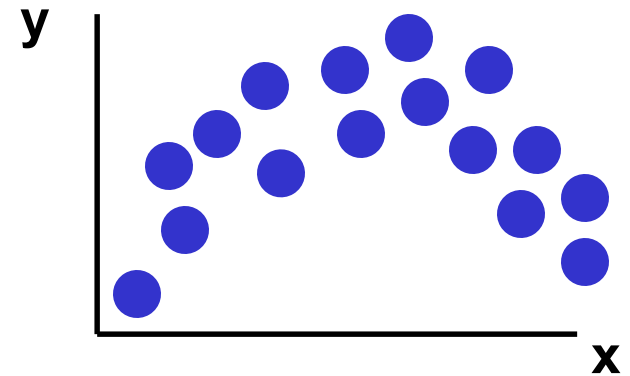


Scatter Plot Examples

Linear relationships



Curvilinear relationships

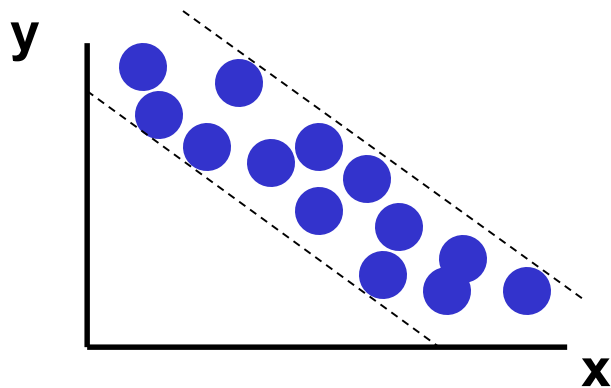
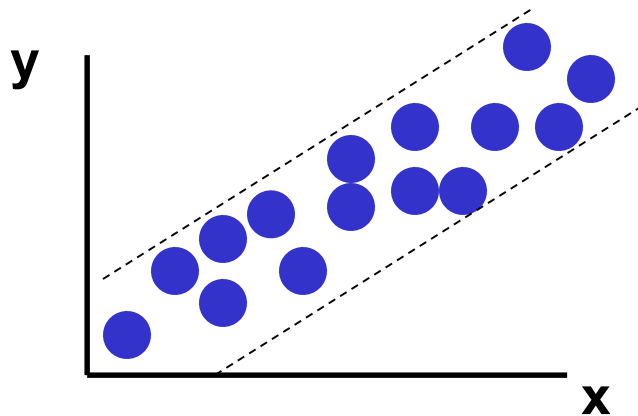




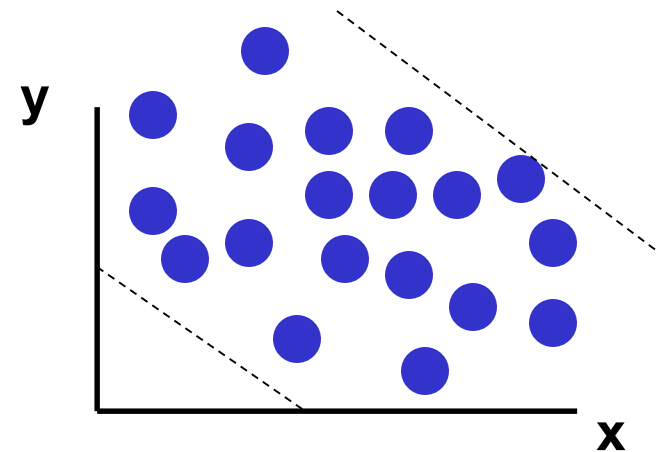
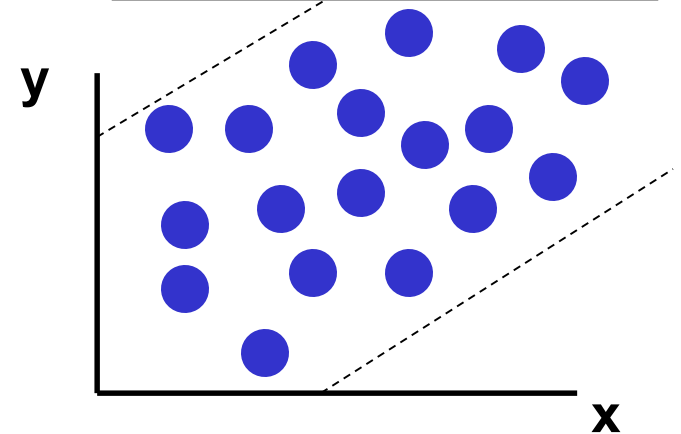
Scatter Plot Examples

(continued)

Strong relationships



Weak relationships

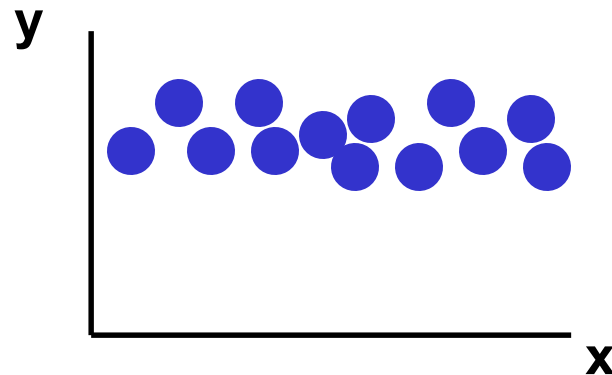
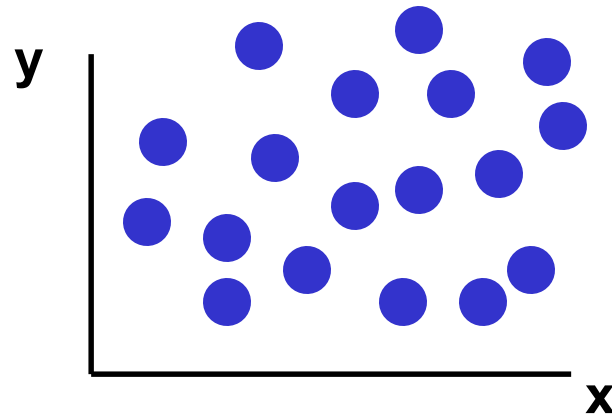




Scatter Plot Examples

(continued)

No relationship





Correlation Coefficient

(continued)

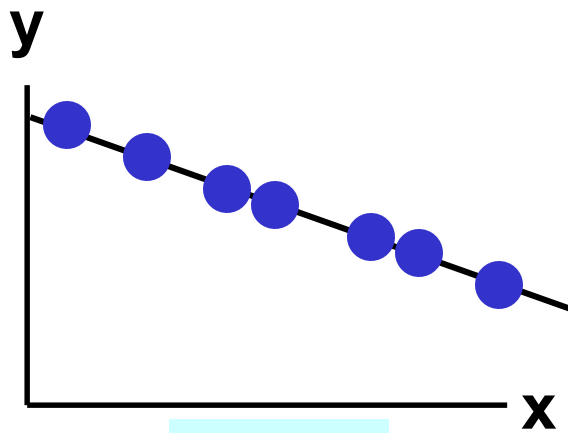
- The **population correlation coefficient ρ** (rho) measures the strength of the association between the variables
- The **sample correlation coefficient r** is an estimate of ρ and is used to measure the strength of the linear relationship in the sample observations



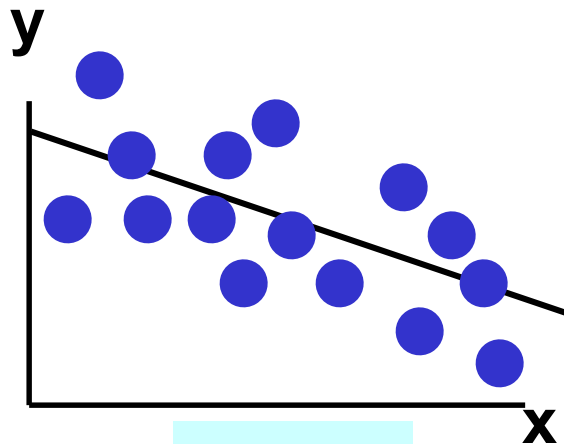
Features of ρ and r

- Unit free
- Range between -1 and 1
- The closer to -1, the stronger the negative linear relationship
- The closer to 1, the stronger the positive linear relationship
- The closer to 0, the weaker the linear relationship

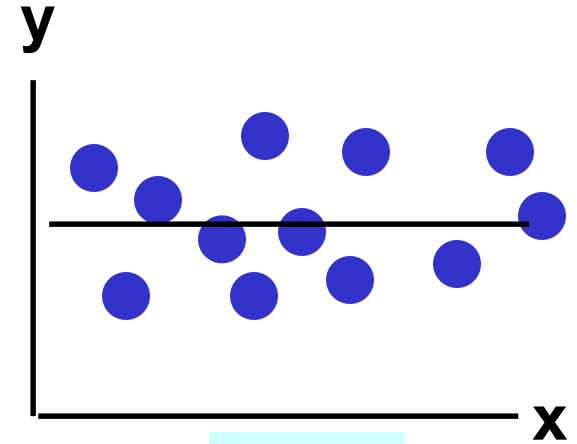
Examples of Approximate r Values



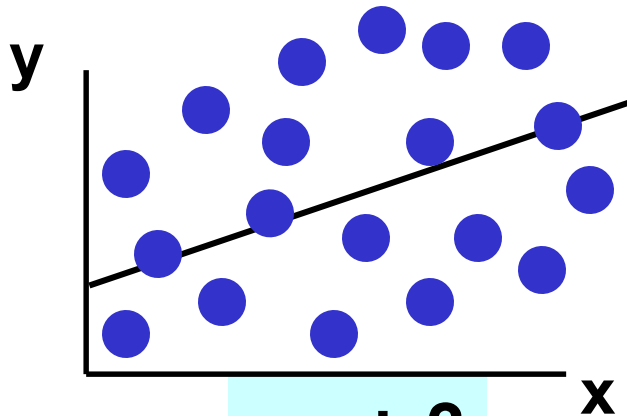
$r = -1$



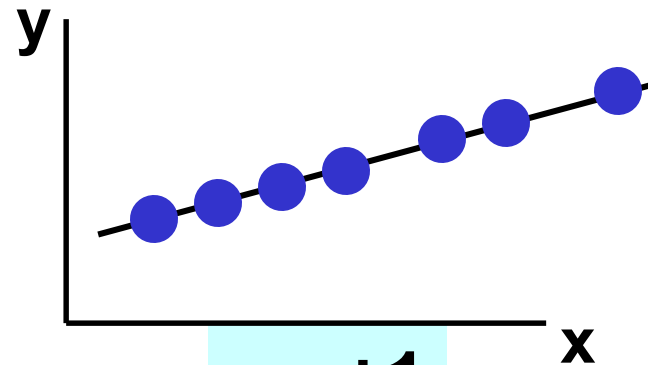
$r = -.6$



$r = 0$



$r = +.3$



$r = +1$



Calculating the Correlation Coefficient

Sample correlation coefficient:

$$r = \frac{\sum (x - \bar{x})(y - \bar{y})}{\sqrt{[\sum (x - \bar{x})^2][\sum (y - \bar{y})^2]}}$$

or the algebraic equivalent:

$$r = \frac{n \sum xy - \sum x \sum y}{\sqrt{[n(\sum x^2) - (\sum x)^2][n(\sum y^2) - (\sum y)^2]}}$$

where:

r = Sample correlation coefficient

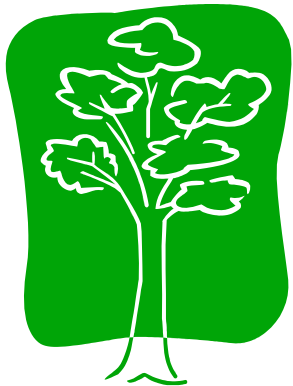
n = Sample size

x = Value of the independent variable

y = Value of the dependent variable

Calculation Example

Tree Height	Trunk Diameter			
y	x	xy	y^2	x^2
35	8	280	1225	64
49	9	441	2401	81
27	7	189	729	49
33	6	198	1089	36
60	13	780	3600	169
21	7	147	441	49
45	11	495	2025	121
51	12	612	2601	144
$\Sigma=321$	$\Sigma=73$	$\Sigma=3142$	$\Sigma=14111$	$\Sigma=713$

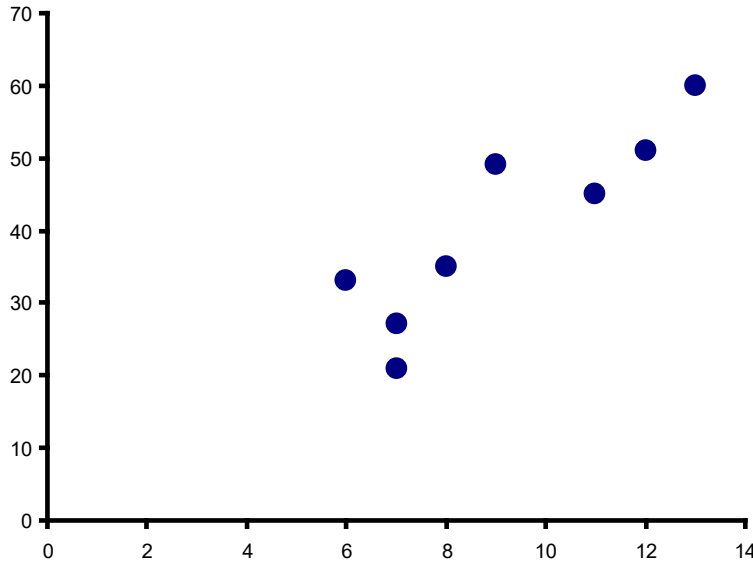




Calculation Example

(continued)

Tree
Height,
y



Trunk Diameter, x

$$\begin{aligned} r &= \frac{n \sum xy - \sum x \sum y}{\sqrt{[n(\sum x^2) - (\sum x)^2][n(\sum y^2) - (\sum y)^2]}} \\ &= \frac{8(3142) - (73)(321)}{\sqrt{[8(713) - (73)^2][8(14111) - (321)^2]}} \\ &= 0.886 \end{aligned}$$

$r = 0.886$ → relatively strong positive linear association between x and y





Excel Output

Excel Correlation Output

Tools / data analysis / correlation...

	Tree Height	Trunk Diameter
Tree Height	1	
Trunk Diameter	0.886231	1

Correlation between
Tree Height and Trunk Diameter





Significance Test for Correlation

- Hypotheses

$$H_0: \rho = 0 \quad (\text{no correlation})$$

$$H_A: \rho \neq 0 \quad (\text{correlation exists})$$

- Test statistic



$$t = \frac{r}{\sqrt{\frac{1-r^2}{n-2}}}$$

(with $n - 2$ degrees of freedom)





Example: Produce Stores

Is there evidence of a linear relationship between tree height and trunk diameter at the .05 level of significance?

$H_0: \rho = 0$ (No correlation)

$H_1: \rho \neq 0$ (correlation exists)

$$\alpha = .05, \quad df = 8 - 2 = 6$$

$$t = \frac{r}{\sqrt{\frac{1-r^2}{n-2}}} = \frac{.886}{\sqrt{\frac{1-.886^2}{8-2}}} = 4.68$$

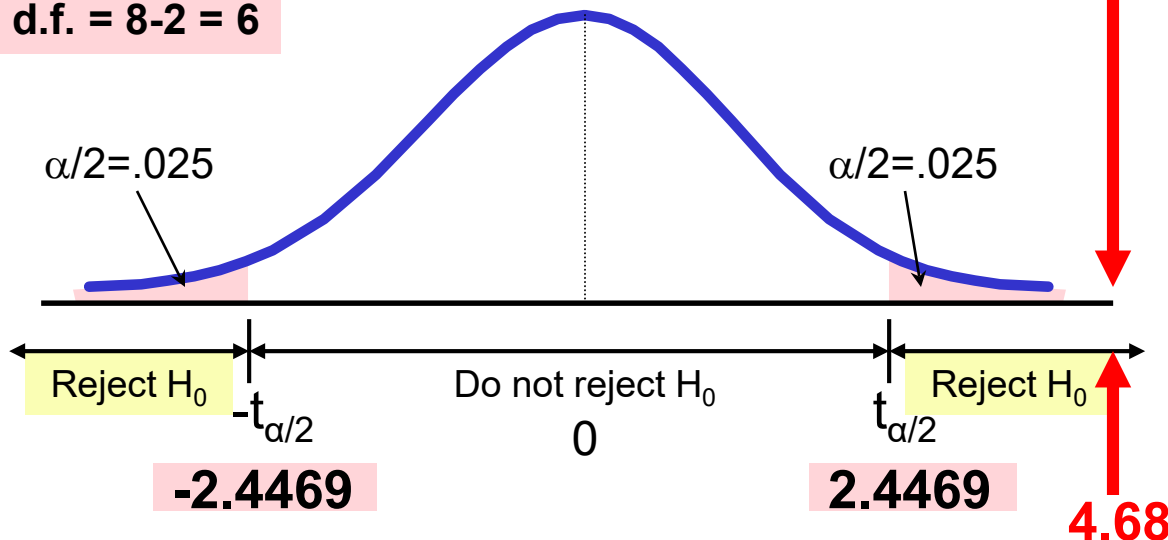




Example: Test Solution

$$t = \frac{r}{\sqrt{\frac{1-r^2}{n-2}}} = \frac{.886}{\sqrt{\frac{1-.886^2}{8-2}}} = 4.68$$

d.f. = 8-2 = 6



Decision:
Reject H_0

Conclusion:
There is **evidence** of a linear relationship at the 5% level of significance



Introduction to Regression Analysis

- **Regression analysis** is used to:
 - Predict the value of a dependent variable based on the value of at least one independent variable
 - Explain the impact of changes in an independent variable on the dependent variable

Dependent variable: the variable we wish to explain

Independent variable: the variable used to explain the dependent variable

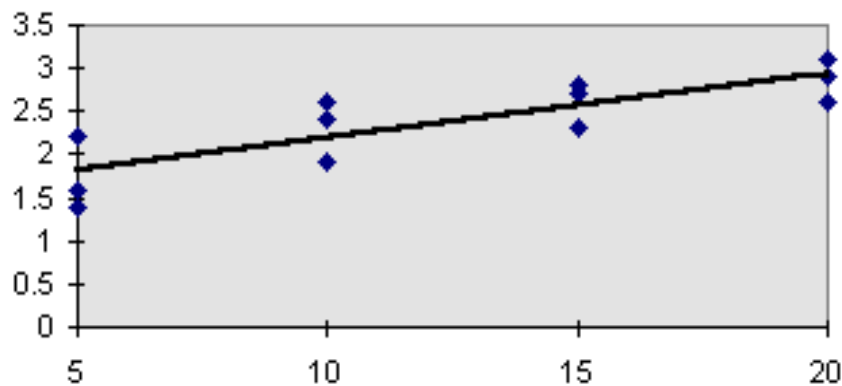


Simple Linear Regression Model

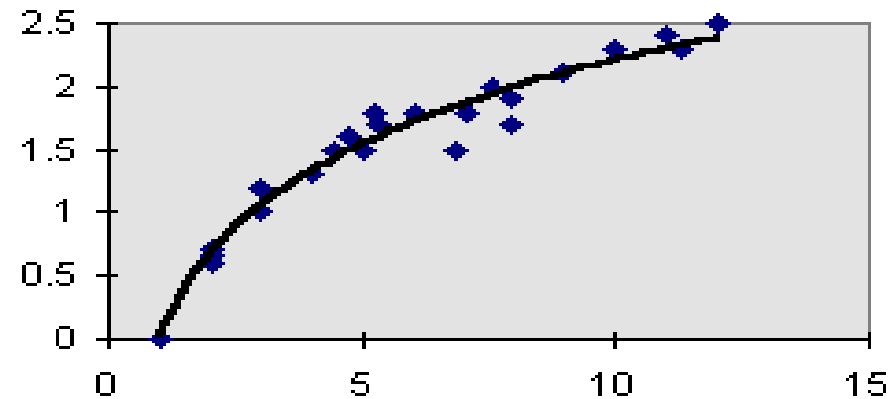
- Only **one independent variable**, x
- Relationship between x and y is described by a linear function
- Changes in y are assumed to be caused by changes in x

Types of Regression Models

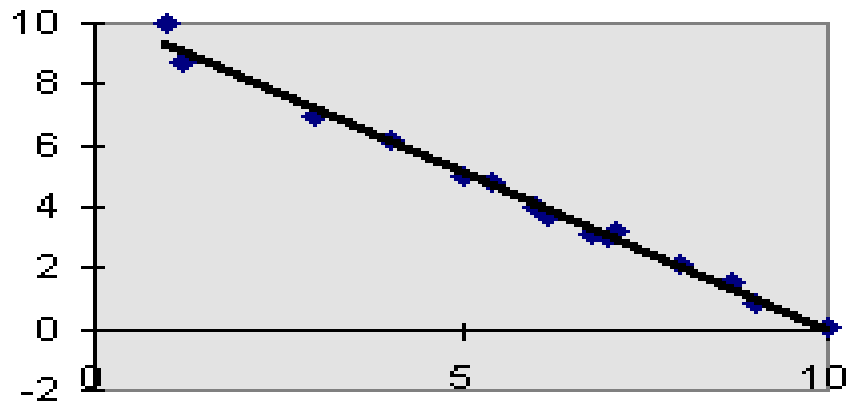
Positive Linear Relationship



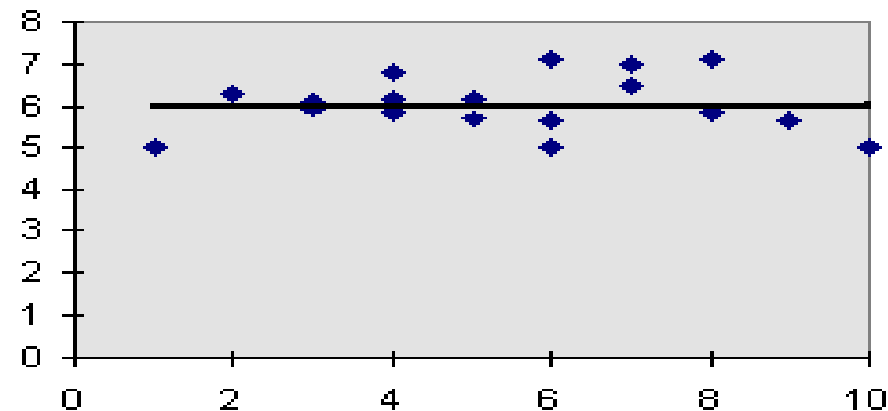
Relationship NOT Linear



Negative Linear Relationship



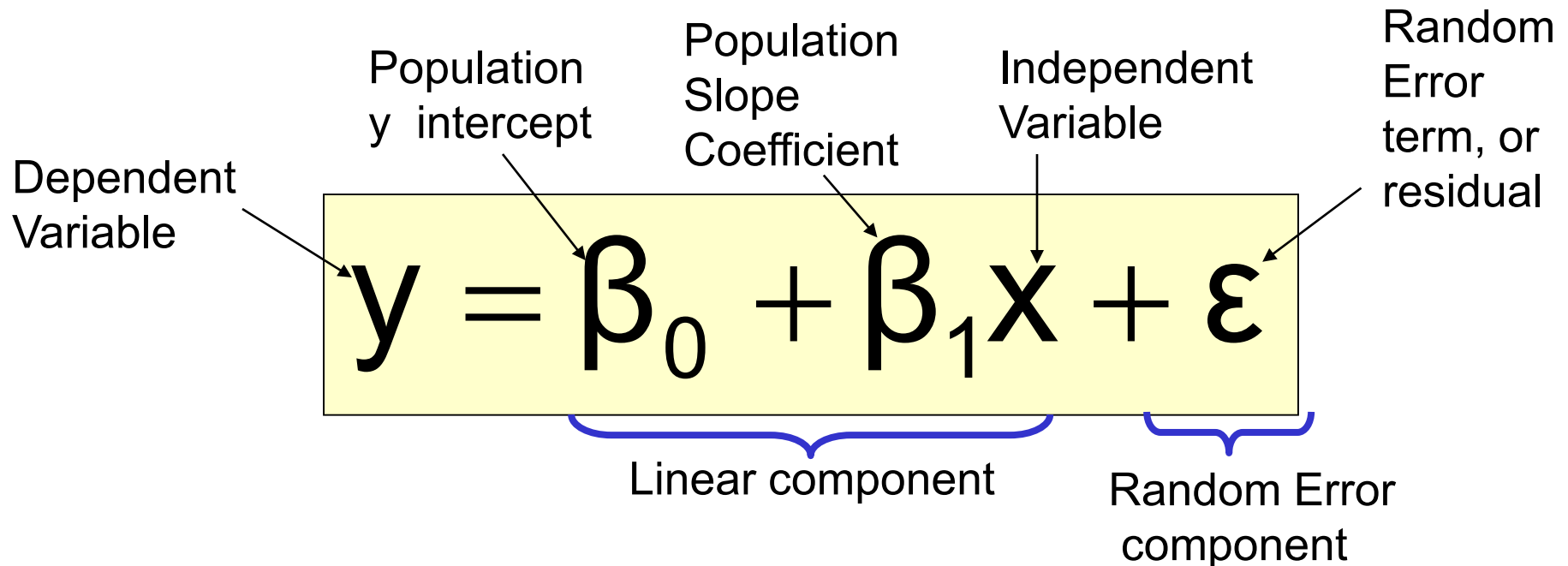
No Relationship





Population Linear Regression

The population regression model:



The diagram illustrates the population regression model equation $y = \beta_0 + \beta_1 x + \epsilon$. The equation is enclosed in a yellow box. Labels with arrows point to specific parts of the equation: 'Dependent Variable' points to y ; 'Population y intercept' points to β_0 ; 'Population Slope Coefficient' points to β_1 ; 'Independent Variable' points to x ; and 'Random Error term, or residual' points to ϵ . Below the equation, two blue brackets identify the components: the 'Linear component' bracket spans from β_0 to x , and the 'Random Error component' bracket spans from ϵ to the right.

$$y = \beta_0 + \beta_1 x + \epsilon$$

Labels and components:

- Dependent Variable: y
- Population y intercept: β_0
- Population Slope Coefficient: β_1
- Independent Variable: x
- Random Error term, or residual: ϵ
- Linear component: $\beta_0 + \beta_1 x$
- Random Error component: ϵ

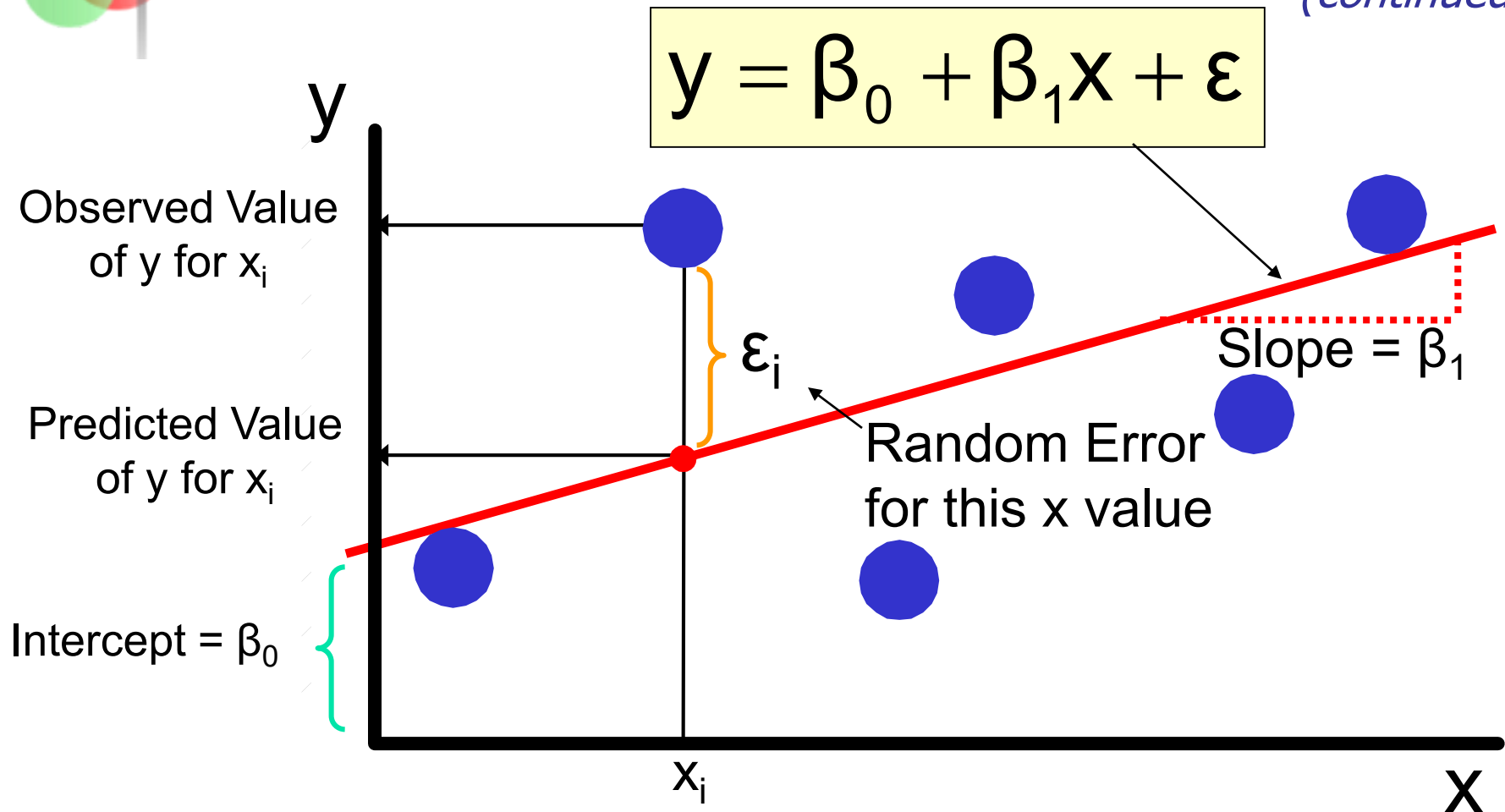


Linear Regression Assumptions

- Error values (ε) are statistically independent
- Error values are normally distributed for any given value of x
- The probability distribution of the errors is normal
- The probability distribution of the errors has constant variance
- The underlying relationship between the x variable and the y variable is linear

Population Linear Regression

(continued)





Estimated Regression Model

The sample regression line provides an **estimate** of the population regression line

Estimated
(or predicted)
y value

Estimate of
the regression
intercept

Estimate of the
regression slope

Independent
variable

$$\hat{y}_i = b_0 + b_1 x$$

The individual random error terms e_i have a mean of zero



Least Squares Criterion

- b_0 and b_1 are obtained by finding the values of b_0 and b_1 that minimize the sum of the squared residuals

$$\begin{aligned}\sum e^2 &= \sum (y - \hat{y})^2 \\ &= \sum (y - (b_0 + b_1 x))^2\end{aligned}$$



The Least Squares Equation

- The formulas for b_1 and b_0 are:

$$b_1 = \frac{\sum (x - \bar{x})(y - \bar{y})}{\sum (x - \bar{x})^2}$$

algebraic equivalent:

$$b_1 = \frac{\sum xy - \frac{\sum x \sum y}{n}}{\sum x^2 - \frac{(\sum x)^2}{n}}$$

and

$$b_0 = \bar{y} - b_1 \bar{x}$$



Interpretation of the Slope and the Intercept

- b_0 is the estimated average value of y when the value of x is zero
- b_1 is the estimated change in the average value of y as a result of a one-unit change in x



Finding the Least Squares Equation

- The coefficients b_0 and b_1 will usually be found using computer software, such as Excel or Minitab
- Other regression measures will also be computed as part of computer-based regression analysis



Simple Linear Regression Example

- A real estate agent wishes to examine the relationship between the selling price of a home and its size (measured in square feet)
- A random sample of 10 houses is selected
 - Dependent variable (y) = house price in \$1000s
 - Independent variable (x) = square feet





Sample Data for House Price Model

House Price in \$1000s (y)	Square Feet (x)
245	1400
312	1600
279	1700
308	1875
199	1100
219	1550
405	2350
324	2450
319	1425
255	1700





Regression Using Excel

■ Tools / Data Analysis / Regression

Microsoft Excel - 13data.xls

File Edit View Insert Format Tools Data Window Help Acrobat

Chart 1

	A	B
1	House Price	Square Feet
2	245	1400
3	312	1600
4	279	1700
5	308	1875
6	199	1100
7	219	1550
8	405	2350
9	324	2450
10	319	1425
11	255	1700
12		
13		
14		
15		

Regression

Input

Input Y Range: \$A\$1:\$A\$11

Input X Range: \$B\$1:\$B\$11

☒ Labels ☐ Constant is Zero

☐ Confidence Level: 95 %

Output options

☐ Output Range:

☒ New Worksheet Ply:

☐ New Workbook

Residuals

☐ Residuals ☐ Residual Plots

☐ Standardized Residuals ☒ Line Fit Plots

Normal Probability

☐ Normal Probability Plots

OK Cancel Help





Excel Output

Regression Statistics

Multiple R	0.76211
R Square	0.58082
Adjusted R Square	0.52842
Standard Error	41.33032
Observations	10

The regression equation is:

$$\text{house price} = 98.24833 + 0.10977 (\text{square feet})$$

ANOVA

	<i>df</i>	<i>SS</i>	<i>MS</i>	<i>F</i>	<i>Significance F</i>
Regression	1	18934.9348	18934.9348	11.0848	0.01039
Residual	8	13665.5652	1708.1957		
Total	9	32600.5000			

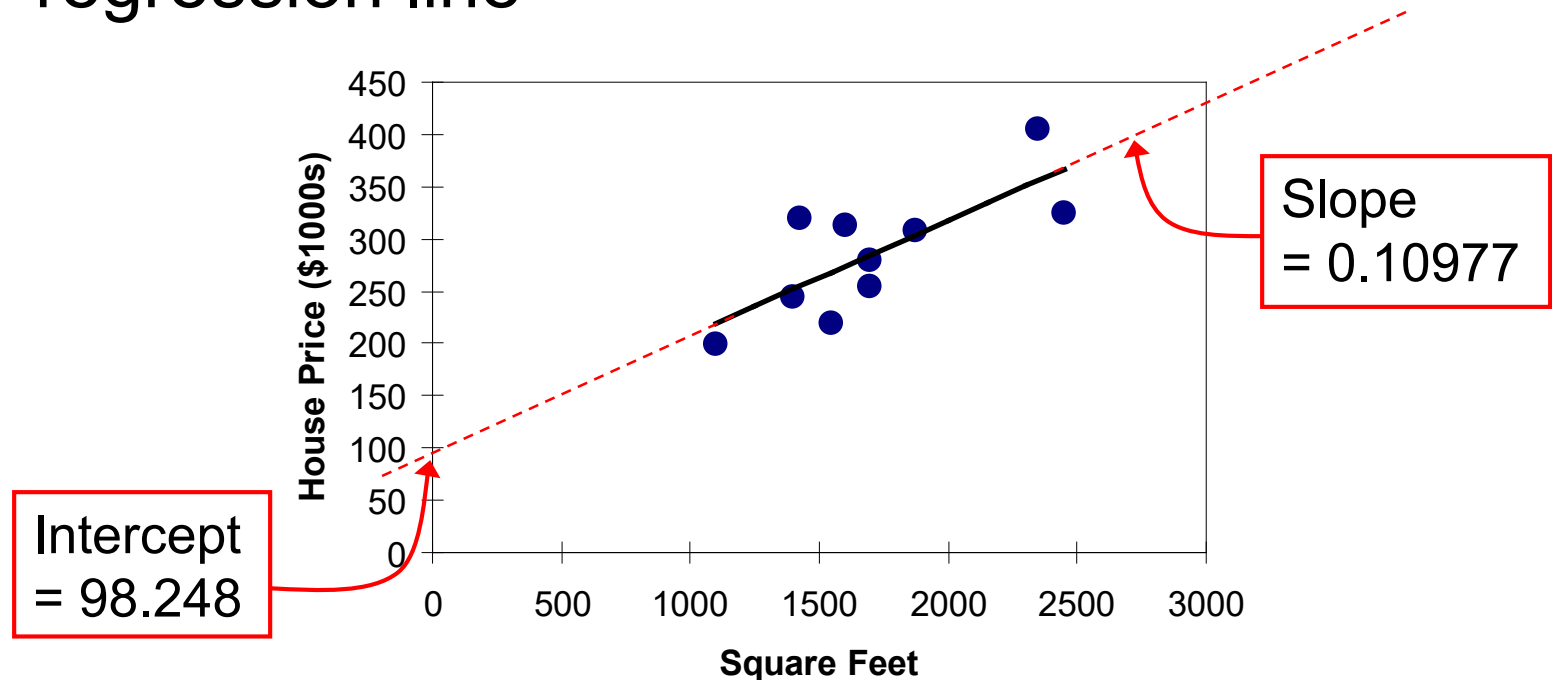
	<i>Coefficients</i>	<i>Standard Error</i>	<i>t Stat</i>	<i>P-value</i>	<i>Lower 95%</i>	<i>Upper 95%</i>
Intercept	98.24833	58.03348	1.69296	0.12892	-35.57720	232.07386
Square Feet	0.10977	0.03297	3.32938	0.01039	0.03374	0.18580





Graphical Presentation

- House price model: scatter plot and regression line



$$\widehat{\text{house price}} = 98.24833 + 0.10977 (\text{square feet})$$



Interpretation of the Intercept, b_0

$$\widehat{\text{house price}} = 98.24833 + 0.10977 (\text{square feet})$$

- b_0 is the estimated average value of Y when the value of X is zero (if $x = 0$ is in the range of observed x values)
 - Here, no houses had 0 square feet, so $b_0 = 98.24833$ just indicates that, for houses within the range of sizes observed, \$98,248.33 is the portion of the house price not explained by square feet





Interpretation of the Slope Coefficient, b_1

$$\widehat{\text{house price}} = 98.24833 + 0.10977(\text{square feet})$$

- b_1 measures the estimated change in the average value of Y as a result of a one-unit change in X
 - Here, $b_1 = .10977$ tells us that the average value of a house increases by $.10977(\$1000) = \109.77 , on average, for each additional one square foot of size





Least Squares Regression Properties

- The sum of the residuals from the least squares regression line is 0 ($\sum (y - \hat{y}) = 0$)
- The sum of the squared residuals is a minimum (minimized $\sum (y - \hat{y})^2$)
- The simple regression line always passes through the mean of the y variable and the mean of the x variable
- The least squares coefficients are unbiased estimates of β_0 and β_1



Explained and Unexplained Variation

- Total variation is made up of two parts:

$$SST = SSE + SSR$$

Total sum of
Squares

Sum of Squares
Error

Sum of Squares
Regression

$$SST = \sum (y - \bar{y})^2$$

$$SSE = \sum (y - \hat{y})^2$$

$$SSR = \sum (\hat{y} - \bar{y})^2$$

where:

\bar{y} = Average value of the dependent variable

y = Observed values of the dependent variable

\hat{y} = Estimated value of y for the given x value



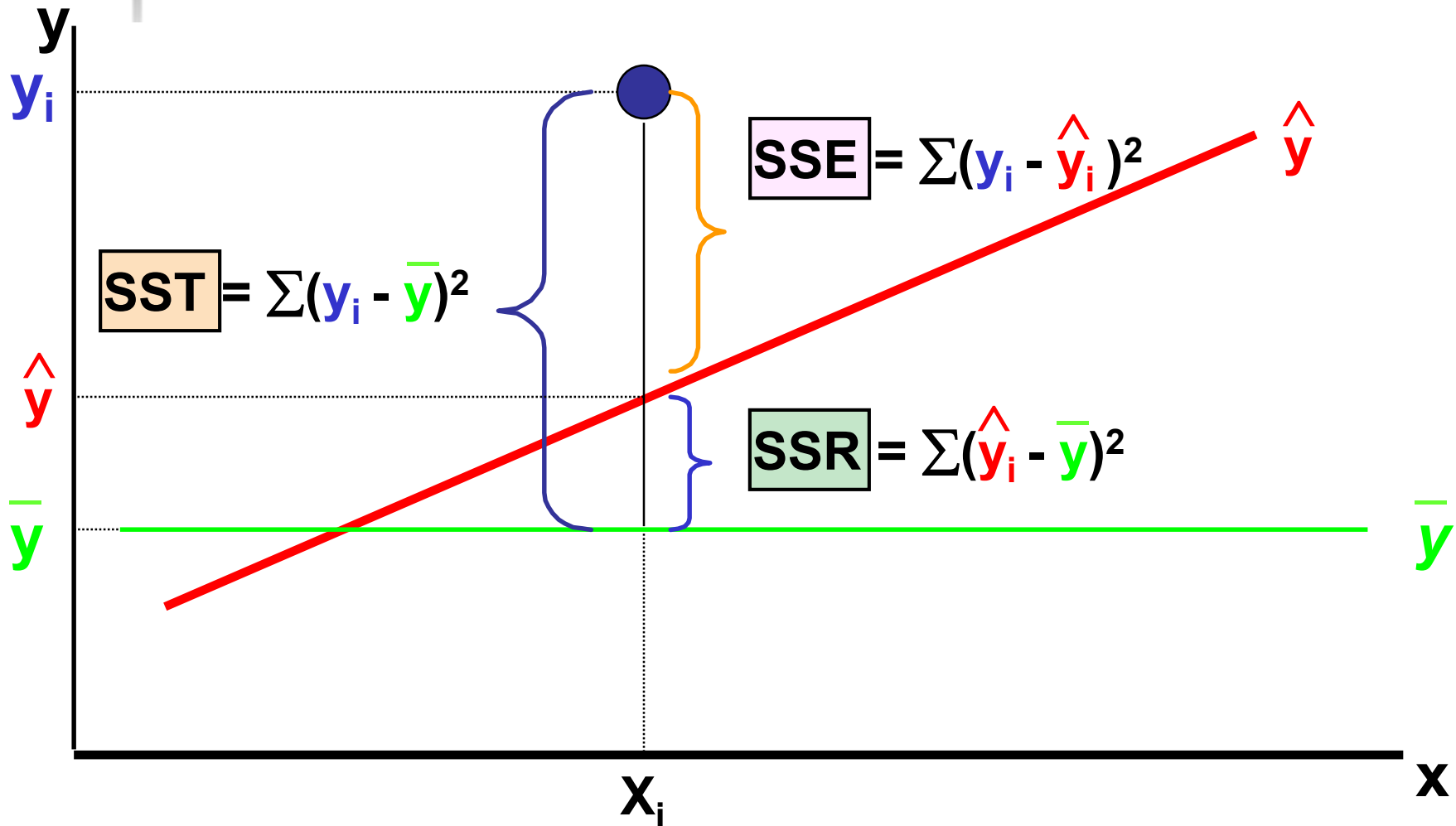
Explained and Unexplained Variation

(continued)

- SST = total sum of squares
 - Measures the variation of the y_i values around their mean y
- SSE = error sum of squares
 - Variation attributable to factors other than the relationship between x and y
- SSR = regression sum of squares
 - Explained variation attributable to the relationship between x and y

Explained and Unexplained Variation

(continued)





Coefficient of Determination, R^2

- The **coefficient of determination** is the portion of the total variation in the dependent variable that is explained by variation in the independent variable
- The coefficient of determination is also called **R-squared** and is denoted as R^2

$$R^2 = \frac{SSR}{SST}$$

where

$$0 \leq R^2 \leq 1$$



Coefficient of Determination, R^2

(continued)

Coefficient of determination

$$R^2 = \frac{SSR}{SST} = \frac{\text{sum of squares explained by regression}}{\text{total sum of squares}}$$

Note: In the single independent variable case, the coefficient of determination is

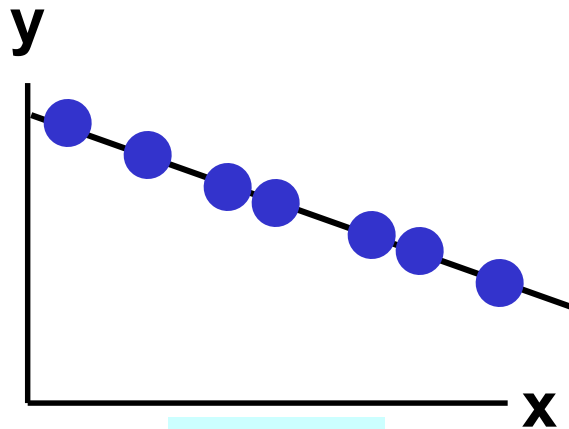
$$R^2 = r^2$$

where:

R^2 = Coefficient of determination

r = Simple correlation coefficient

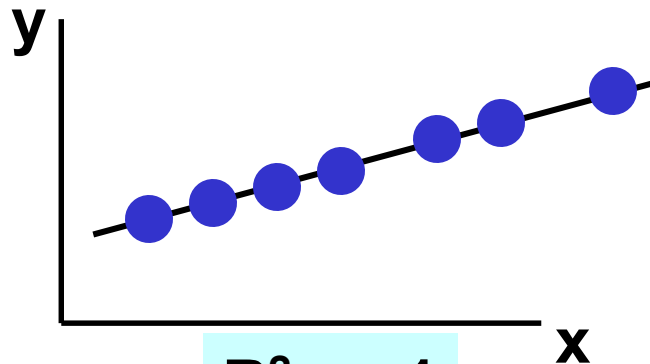
Examples of Approximate R^2 Values



$$R^2 = 1$$

$$R^2 = 1$$

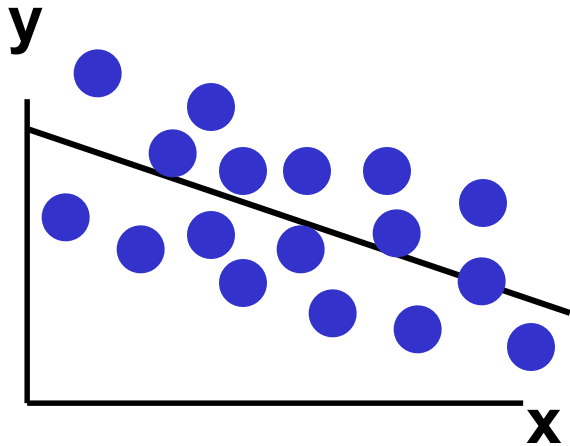
**Perfect linear relationship
between x and y:**



$$R^2 = +1$$

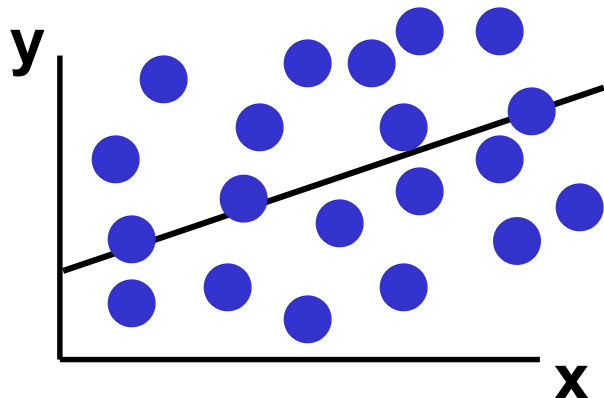
**100% of the variation in y is
explained by variation in x**

Examples of Approximate R^2 Values



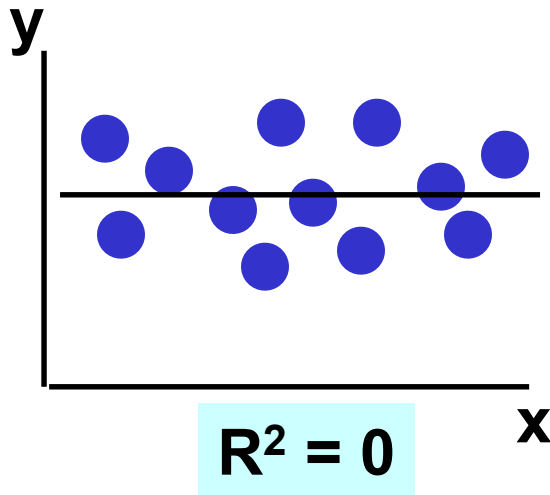
$$0 < R^2 < 1$$

**Weaker linear relationship
between x and y:**



**Some but not all of the
variation in y is explained
by variation in x**

Examples of Approximate R^2 Values



$$R^2 = 0$$

**No linear relationship
between x and y:**

**The value of Y does not
depend on x. (None of the
variation in y is explained
by variation in x)**



Excel Output

Regression Statistics

Multiple R	0.76211
R Square	0.58082
Adjusted R Square	0.52842
Standard Error	41.33032
Observations	10

$$R^2 = \frac{SSR}{SST} = \frac{18934.9348}{32600.5000} = 0.58082$$

58.08% of the variation in house prices is explained by variation in square feet

ANOVA

	<i>df</i>	SS	<i>MS</i>	<i>F</i>	<i>Significance F</i>
Regression	1	18934.9348	18934.9348	11.0848	0.01039
Residual	8	13665.5652	1708.1957		
Total	9	32600.5000			

	<i>Coefficients</i>	<i>Standard Error</i>	<i>t Stat</i>	<i>P-value</i>	<i>Lower 95%</i>	<i>Upper 95%</i>
Intercept	98.24833	58.03348	1.69296	0.12892	-35.57720	232.07386
Square Feet	0.10977	0.03297	3.32938	0.01039	0.03374	0.18580





Standard Error of Estimate

- The standard deviation of the variation of observations around the regression line is estimated by

$$s_{\varepsilon} = \sqrt{\frac{SSE}{n - k - 1}}$$

Where

SSE = Sum of squares error

n = Sample size

k = number of independent variables in the model



The Standard Deviation of the Regression Slope

- The standard error of the regression slope coefficient (b_1) is estimated by

$$s_{b_1} = \frac{s_\varepsilon}{\sqrt{\sum (x - \bar{x})^2}} = \frac{s_\varepsilon}{\sqrt{\sum x^2 - \frac{(\sum x)^2}{n}}}$$

where:

s_{b_1} = Estimate of the standard error of the least squares slope

$s_\varepsilon = \sqrt{\frac{SSE}{n-2}}$ = Sample standard error of the estimate



Excel Output

Regression Statistics

Multiple R	0.76211
R Square	0.58082
Adjusted R Square	0.52842
Standard Error	41.33032
Observations	10

$$s_{\varepsilon} = 41.33032$$

$$s_{b_1} = 0.03297$$

ANOVA

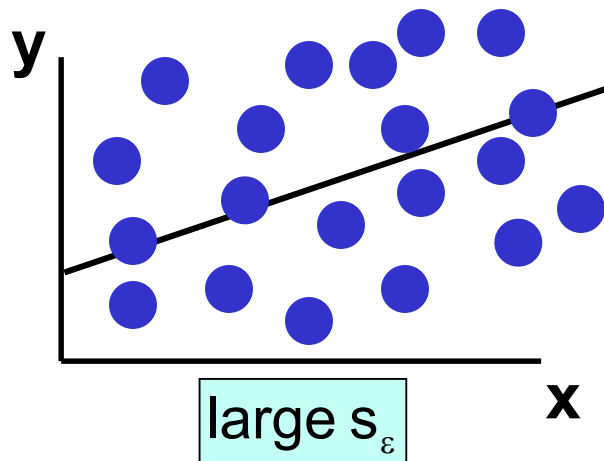
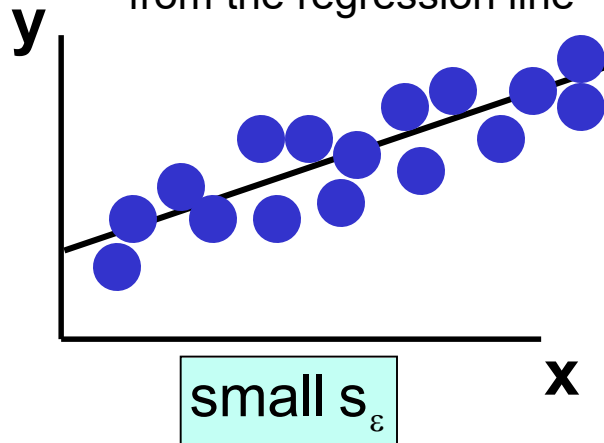
	<i>df</i>	<i>SS</i>	<i>MS</i>	<i>F</i>	<i>Significance F</i>
Regression	1	18934.9348	18934.9348	11.0848	0.01039
Residual	8	13665.5652	1708.1957		
Total	9	32600.5000			

	<i>Coefficients</i>	<i>Standard Error</i>	<i>t Stat</i>	<i>P-value</i>	<i>Lower 95%</i>	<i>Upper 95%</i>
Intercept	98.24833	58.03348	1.69296	0.12892	-35.57720	232.07386
Square Feet	0.10977	0.03297	3.32938	0.01039	0.03374	0.18580

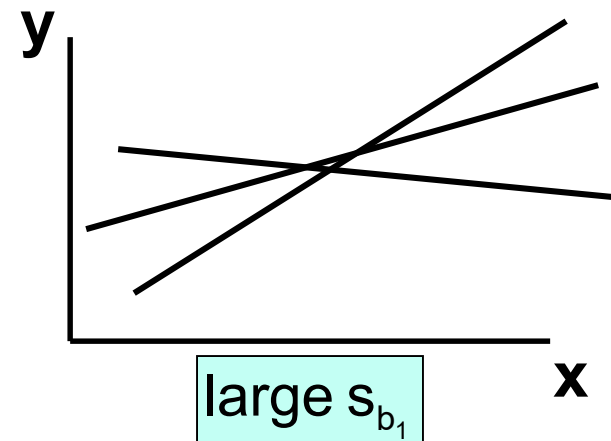
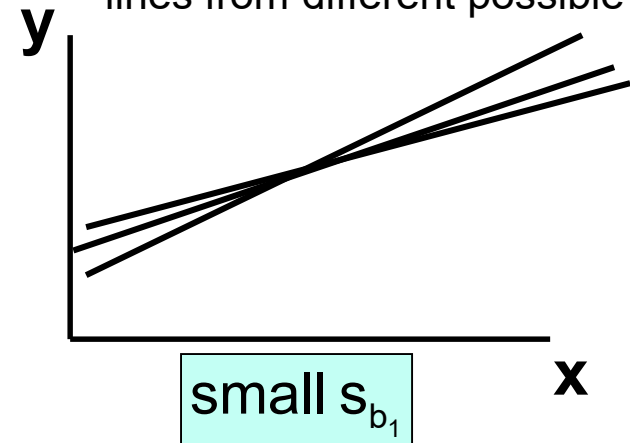


Comparing Standard Errors

Variation of observed y values
from the regression line



Variation in the slope of regression
lines from different possible samples





Inference about the Slope: t Test

- t test for a population slope
 - Is there a linear relationship between x and y?
- Null and alternative hypotheses
 - $H_0: \beta_1 = 0$ (no linear relationship)
 - $H_1: \beta_1 \neq 0$ (linear relationship does exist)
- Test statistic

■

$$t = \frac{b_1 - \beta_1}{s_{b_1}}$$

■

$$\text{d.f.} = n - 2$$

where:

b_1 = Sample regression slope coefficient

β_1 = Hypothesized slope

s_{b_1} = Estimator of the standard error of the slope

Inference about the Slope: t Test

(continued)

House Price in \$1000s (y)	Square Feet (x)
245	1400
312	1600
279	1700
308	1875
199	1100
219	1550
405	2350
324	2450
319	1425
255	1700

Estimated Regression Equation:

$$\widehat{\text{house price}} = 98.25 + 0.1098 (\text{sq.ft.})$$

The slope of this model is 0.1098

Does square footage of the house
affect its sales price?



Inferences about the Slope: t Test Example

Test Statistic: **$t = 3.329$**

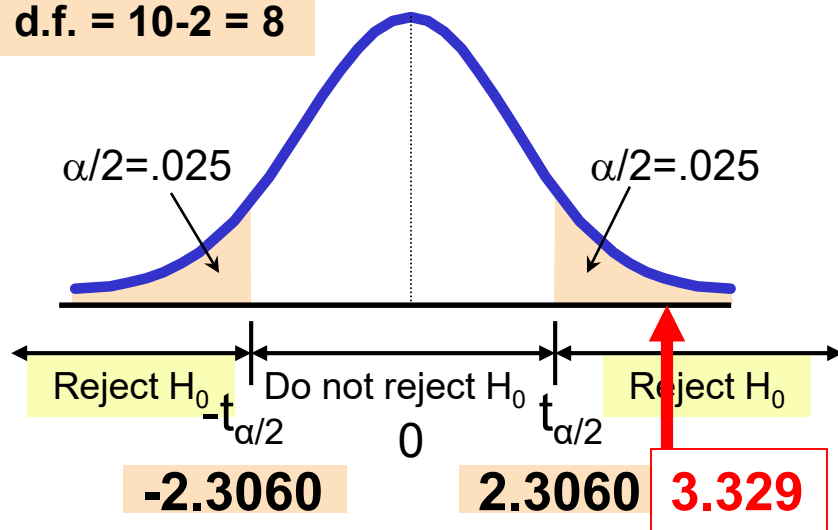
$$H_0: \beta_1 = 0$$

$$H_A: \beta_1 \neq 0$$

From Excel output:

	<i>Coefficients</i>	<i>Standard Error</i>	<i>t Stat</i>	<i>P-value</i>
Intercept	98.24833	58.03348	1.69296	0.12892
Square Feet	0.10977	0.03297	3.32938	0.01039

$$\text{d.f.} = 10 - 2 = 8$$



Decision:

Reject H_0

Conclusion:

There is sufficient evidence that square footage affects house price



Regression Analysis for Description

Confidence Interval Estimate of the Slope:

$$b_1 \pm t_{\alpha/2} s_{b_1}$$

$$\text{d.f.} = n - 2$$

Excel Printout for House Prices:

	<i>Coefficients</i>	<i>Standard Error</i>	<i>t Stat</i>	<i>P-value</i>	<i>Lower 95%</i>	<i>Upper 95%</i>
Intercept	98.24833	58.03348	1.69296	0.12892	-35.57720	232.07386
Square Feet	0.10977	0.03297	3.32938	0.01039	0.03374	0.18580

At 95% level of confidence, the confidence interval for the slope is (0.0337, 0.1858)



Regression Analysis for Description

	<i>Coefficients</i>	<i>Standard Error</i>	<i>t Stat</i>	<i>P-value</i>	<i>Lower 95%</i>	<i>Upper 95%</i>
Intercept	98.24833	58.03348	1.69296	0.12892	-35.57720	232.07386
Square Feet	0.10977	0.03297	3.32938	0.01039	0.03374	0.18580

Since the units of the house price variable is \$1000s, we are 95% confident that the average impact on sales price is between \$33.70 and \$185.80 per square foot of house size

This 95% confidence interval **does not include 0**.

Conclusion: There is a significant relationship between house price and square feet at the .05 level of significance



Confidence Interval for the Average y , Given x

Confidence interval estimate for the **mean of y** given a particular x_p

Size of interval varies according to distance away from mean, \bar{x}

$$\hat{y} \pm t_{\alpha/2} s_{\varepsilon} \sqrt{\frac{1}{n} + \frac{(x_p - \bar{x})^2}{\sum (x - \bar{x})^2}}$$



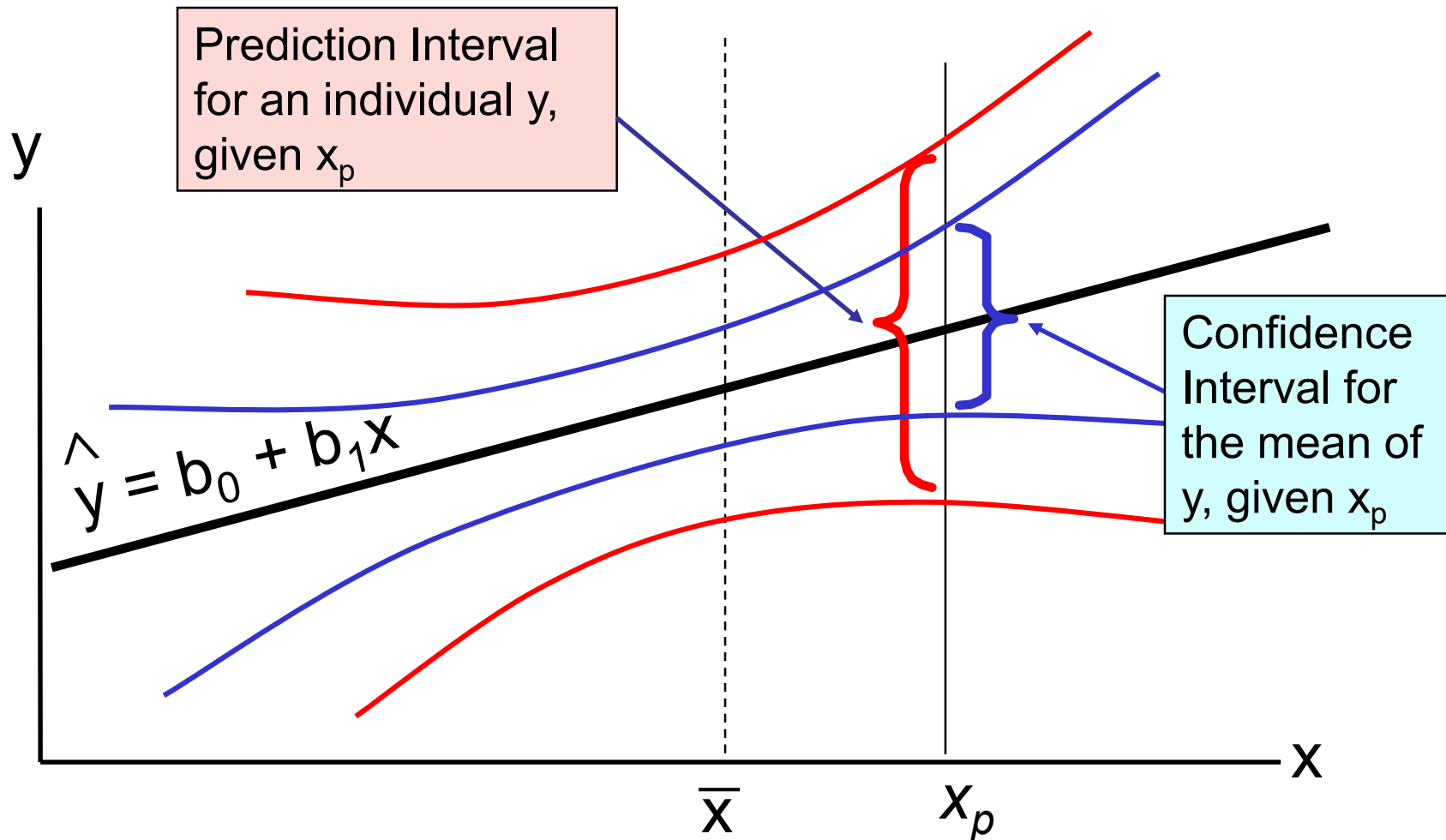
Confidence Interval for an Individual y , Given x

Confidence interval estimate for an **Individual value of y** given a particular x_p

$$\hat{y} \pm t_{\alpha/2} s_{\varepsilon} \sqrt{1 + \frac{1}{n} + \frac{(x_p - \bar{x})^2}{\sum (x - \bar{x})^2}}$$

This extra term adds to the interval width to reflect the added uncertainty for an individual case

Interval Estimates for Different Values of x





Example: House Prices

House Price in \$1000s (y)	Square Feet (x)
245	1400
312	1600
279	1700
308	1875
199	1100
219	1550
405	2350
324	2450
319	1425
255	1700

Estimated Regression Equation:

$$\widehat{\text{house price}} = 98.25 + 0.1098 (\text{sq.ft.})$$

Predict the price for a house
with 2000 square feet





Example: House Prices

(continued)

Predict the price for a house with 2000 square feet:

$$\begin{aligned}\widehat{\text{house price}} &= 98.25 + 0.1098 (\text{sq.ft.}) \\ &= 98.25 + 0.1098(2000) \\ &= 317.85\end{aligned}$$

The predicted price for a house with 2000 square feet is $317.85(\$1,000\text{s}) = \$317,850$





Estimation of Mean Values: Example

Confidence Interval Estimate for $E(y)|x_p$

Find the 95% confidence interval for the average price of 2,000 square-foot houses

Predicted Price $\hat{Y}_i = 317.85$ (\$1,000s)

$$\hat{y} \pm t_{\alpha/2} s_{\varepsilon} \sqrt{\frac{1}{n} + \frac{(x_p - \bar{x})^2}{\sum (x - \bar{x})^2}} = 317.85 \pm 37.12$$

The confidence interval endpoints are 280.66 -- 354.90, or from \$280,660 -- \$354,900



Estimation of Individual Values: Example

Prediction Interval Estimate for $y|x_p$

Find the 95% confidence interval for an individual house with 2,000 square feet

Predicted Price $\hat{Y}_i = 317.85$ (\$1,000s)

$$\hat{y} \pm t_{\alpha/2} s_{\varepsilon} \sqrt{1 + \frac{1}{n} + \frac{(x_p - \bar{x})^2}{\sum (x - \bar{x})^2}} = 317.85 \pm 102.28$$

The prediction interval endpoints are 215.50 -- 420.07,
or from \$215,500 -- \$420,070



Finding Confidence and Prediction Intervals PHStat

- In Excel, use

PHStat | regression | simple linear regression ...

- Check the

“confidence and prediction interval for $X=$ ”

box and enter the x-value and confidence level desired

Finding Confidence and Prediction Intervals PHStat

(continued)

	A	B
1	Confidence Interval Estimate	
2		
3	Data	
4	X Value	2000
5	Confidence Level	95%
6		
7	Intermediate Calculations	
8	Sample Size	10
9	Degrees of Freedom	8
10	t Value	2.306006
11	Sample Mean	1715
12	Sum of Squared Difference	1571500
13	Standard Error of the Estimate	41.33032
14	h Statistic	0.151686
15	Average Predicted Y (YHat)	317.7838
16		
17	For Average Predicted Y (YHat)	
18	Interval Half Width	37.11952
19	Confidence Interval Lower Limit	280.6643
20	Confidence Interval Upper Limit	354.9033
21		
22	For Individual Response Y	
23	Interval Half Width	102.2813
24	Prediction Interval Lower Limit	215.5025
25	Prediction Interval Upper Limit	420.0651

Input values

Confidence Interval Estimate for $E(y)|x_p$

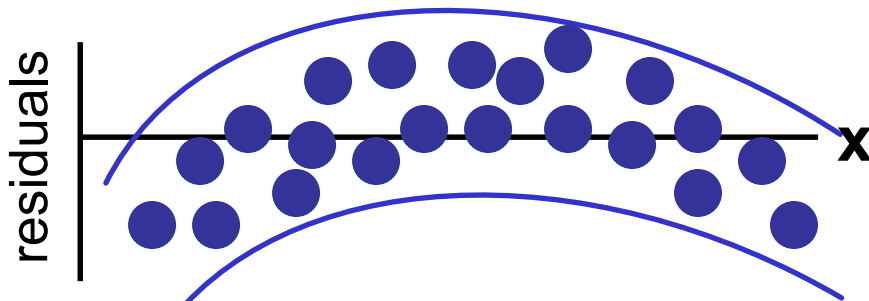
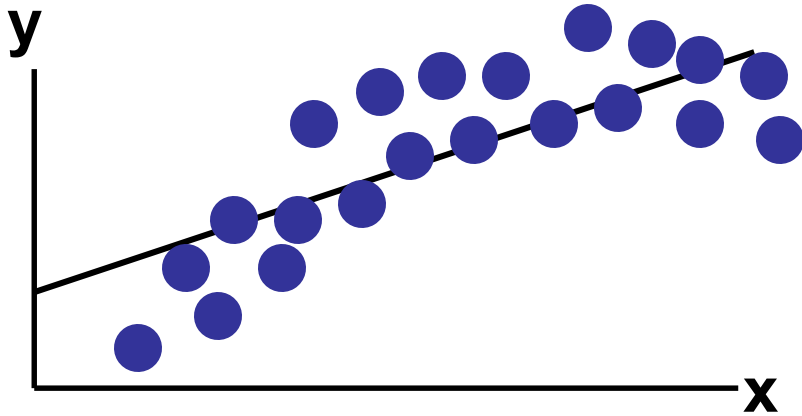
Prediction Interval Estimate for $y|x_p$



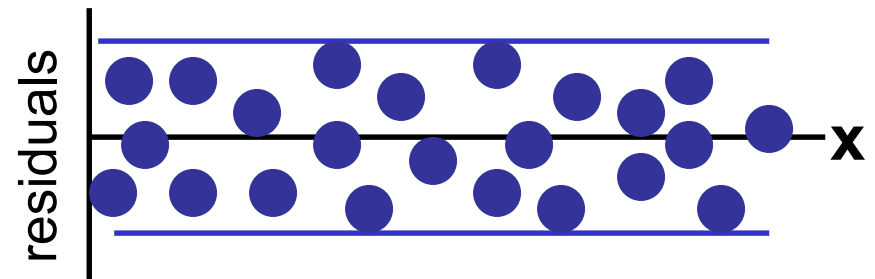
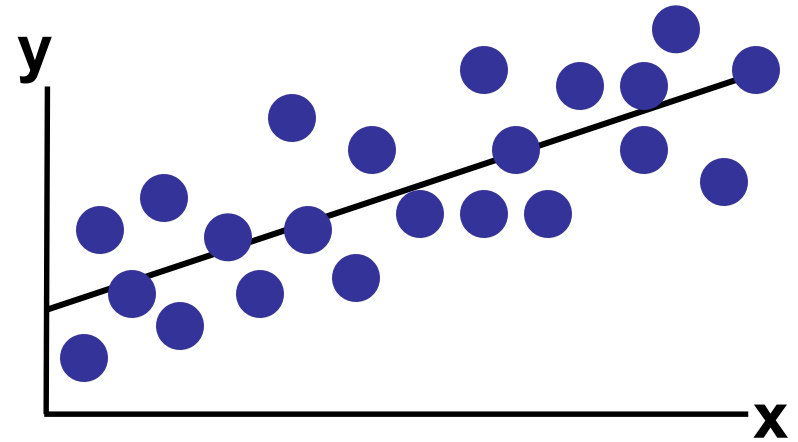
Residual Analysis

- Purposes
 - Examine for linearity assumption
 - Examine for constant variance for all levels of x
 - Evaluate normal distribution assumption
- Graphical Analysis of Residuals
 - Can plot residuals vs. x
 - Can create histogram of residuals to check for normality

Residual Analysis for Linearity

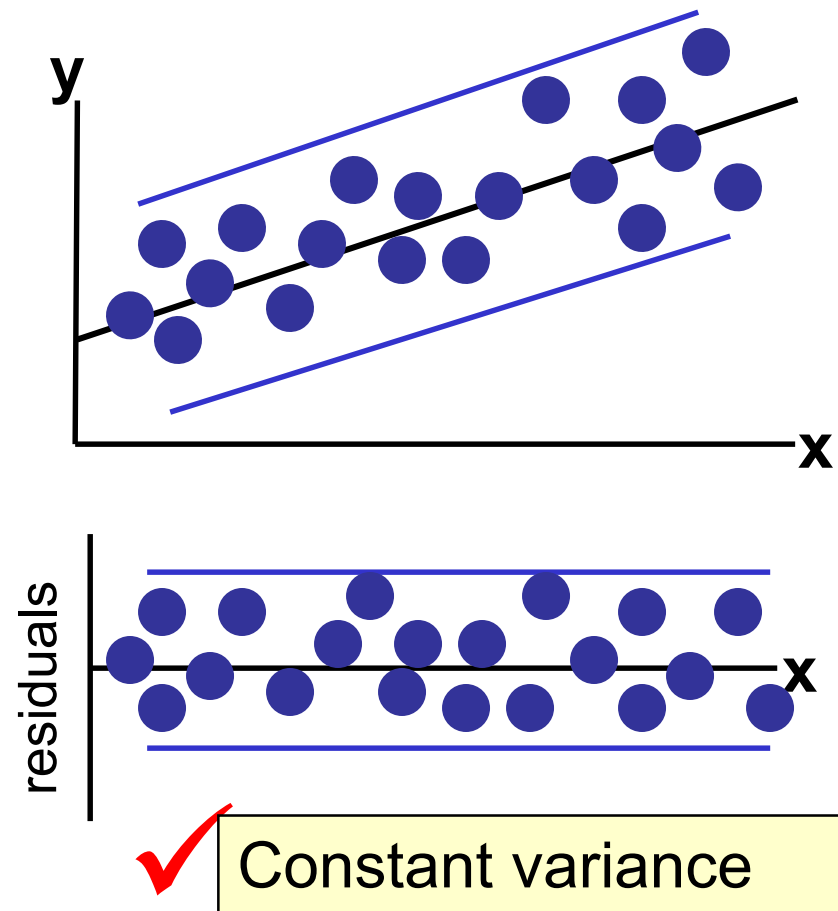
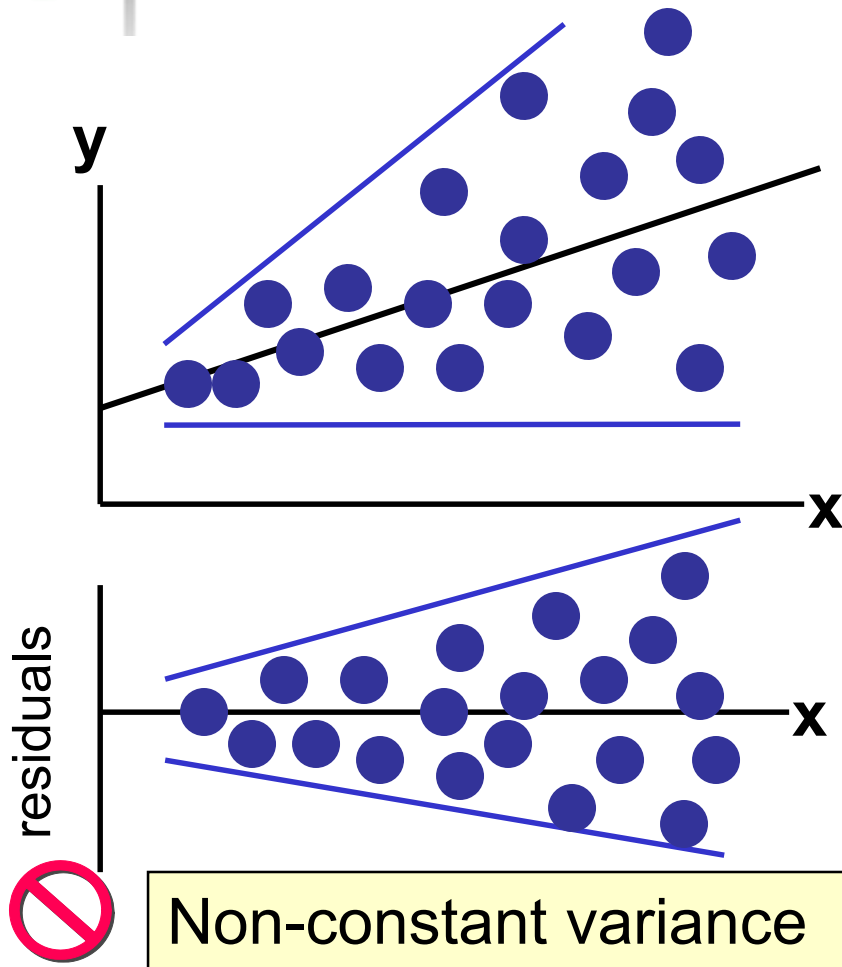


Not Linear



Linear

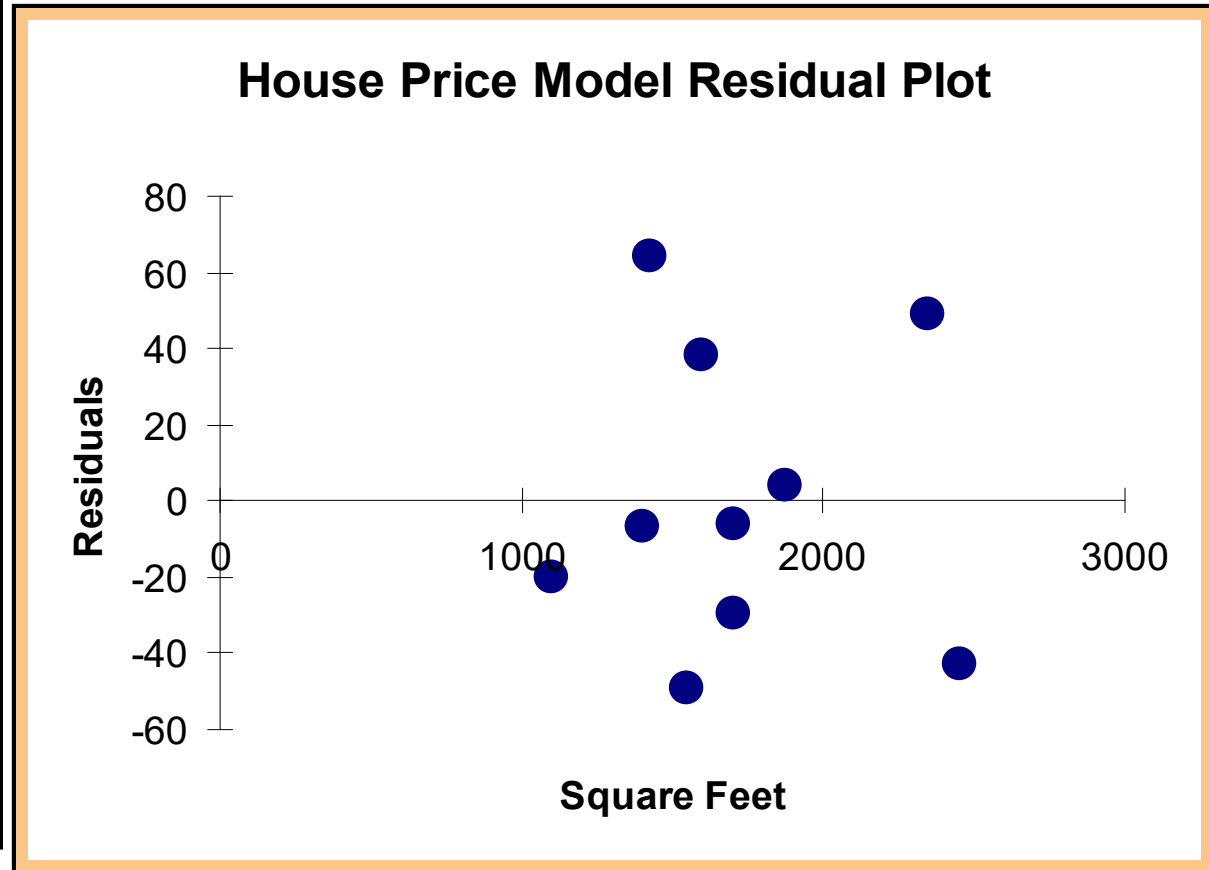
Residual Analysis for Constant Variance





Excel Output

RESIDUAL OUTPUT		
	<i>Predicted House Price</i>	<i>Residuals</i>
1	251.92316	-6.923162
2	273.87671	38.12329
3	284.85348	-5.853484
4	304.06284	3.937162
5	218.99284	-19.99284
6	268.38832	-49.38832
7	356.20251	48.79749
8	367.17929	-43.17929
9	254.6674	64.33264
10	284.85348	-29.85348





Chapter Summary

- Introduced correlation analysis
- Discussed correlation to measure the strength of a linear association
- Introduced simple linear regression analysis
- Calculated the coefficients for the simple linear regression equation
- Described measures of variation (R^2 and s_ϵ)
- Addressed assumptions of regression and correlation



Chapter Summary

(continued)

- Described inference about the slope
- Addressed estimation of mean values and prediction of individual values
- Discussed residual analysis